## $A Q A$

# General Certificate of Secondary Education November 2012 

Mathematics (Linear) B<br>4365 Paper 1

Higher Tier

# Final 

Mark Scheme

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## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

Mdep A method mark dependent on a previous method mark being awarded.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
Bdep A mark that can only be awarded if a previous independent mark has been awarded.

Q Marks awarded for quality of written communication. (QWC)
ft Follow through marks. Marks awarded following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
oe $\quad$ Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$
[a,b] Accept values between $a$ and $b$ inclusive.

## Paper 1 Higher Tier

| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 1(a) | 64 | B1 |  |
| :--- | :--- | :---: | :--- |
| $\mathbf{1 ( b )}$ 116 B1  <br> $\mathbf{1}(\mathbf{c})$ Corresponding B1  |  |  |  |


| 2(a) | Fills in totals on grid for at least 3 <br> correct 9s | M1 |  |
| :--- | :--- | :---: | :--- |
|  | 9 | A1 |  |


| Alt <br> 2(a) | Identifies 9 as most likely total <br> eg $(1,8),(2,7),(7,2)$ etc.. for at <br> least 3 totals | M1 |  |
| :---: | :--- | :---: | :--- |
|  | 9 | A1 | $8 / 64$ is A0 even if 9 stated |


| 2(b) | Fills in 4,5 or 6 correct totals on grid <br> for $2,3,15$ and 16 | M1 | Identifies at least 4 of (1, 1), (1, 2), (2, 1), <br> $(7,8),(8,7)$ or $(8,8)$ with no wrong pairs. <br> Need not be as a bracket, $1+1$ is OK for <br> example. Totals need not be seen. |
| :---: | :--- | :---: | :--- |
|  | Denominator of 64 or numerator of 6 | M1 | 64 choices identified |


| Alt <br> 2(b) | $\frac{1}{8} \times \frac{1}{8}$ | M1 |  |
| :---: | :--- | :--- | :--- |
|  | $6 \times \frac{1}{8} \times \frac{1}{8}$ | M1 | oe |
|  | $\frac{6}{64}$ | A1 | oe |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 3 | Fully labelled diagram with angles <br> Half-Marathon $90^{\circ}$ <br> 5 K $126^{\circ}$ <br> 10K $72^{\circ}$ <br> Marathon $72^{\circ}$ <br> tolerance $\pm 2^{\circ}$ for drawing  | B4 | B3 Angles correct but not labelled or wrongly labelled or angles correctly calculated and labelled but wrongly drawn. <br> Part Marks to maximum of 3 <br> B1 Half Marathon $90^{\circ}$ and labelled <br> B1 10K and Marathon equal angles or equal angles stated but drawn wrongly and labelled. <br> B1 $5 \mathrm{~K} 126^{\circ}$ and labelled <br> The following only to be awarded if nothing drawn, or if working scores more than the diagram. <br> B1 Working to show each angle for women $=18^{\circ}$. <br> B1 all correct numbers of women in each category calculated, ie 5 for $\mathrm{HM}, 7$ for 5 K , 4 each for $5 K$ and $M$. |


| 4(a) | Translation and 7 right, 2 down or $\binom{7}{-2}$ | B2 | B1 Translation <br> B1 7 right or $7 \rightarrow$ or $\binom{7}{y}$ <br> B1 2 down $2 \downarrow$ or $\binom{x}{-2}$ <br> B1 $\binom{-7}{2}$ or $\binom{-2}{7}$ or $(7,-2)$ |
| :---: | :---: | :---: | :---: |




| Q | Answer | Mark | Comments |
| :---: | :--- | :---: | :--- |
| Alt <br> $\mathbf{9}$   Guess a value and multiplies <br> correctly by 16 <br>  M1 <br>  <br> Guesses a second value nearer to or <br> bracket the correct answer and <br> multiplies correctly by 16 M1dep $x=1$ gives 16 <br> $x=2$ gives 32 <br>  1.5 (oe) or 9 after 1.5 seen A1 oe |  |  |  |



| Q Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 11(a) | (Angle $A D B=) 90-50$ or 180-(90 <br> $+50)(=40)$ | M1 | May be on diagram. Accept $D=40$ or <br> obtuse angle at $D$ marked or labelled as <br> 140. |
| :---: | :--- | :---: | :--- |
|  | $(180-$ Their $C D B) \div 2$ <br> or their $A D B \div 2$ | M1dep | Their CDB must be from $180-$ their $A D B$ <br> Must be complete method |
|  | 20 | A1 | May be on diagram |


| Alt | $50+y+y=90$ | M1 | oe $90+50+y+y=180$ |
| :---: | :--- | :---: | :--- |
| 11(a) | $2 y=40$ | M1 | $y=(180-140) \div 2$ |
|  | 20 | A1 |  |


| $11(b)$ | (tri) Angle in semi-circle $\left(=90^{\circ}\right)$ <br> or (tri) Angle on diameter is $90^{\circ}$ | Q1 | Strand (i) |
| :---: | :--- | :--- | :--- |


| 12(a) | 2.5 or $\frac{5}{2}$ | B1 | oe accept $1: 2.5$ or $2: 5$ <br> Incorrect cancelling of $15 / 6$ is B0. |
| :---: | :--- | :---: | :--- |
| 12(b) | 60 | B1 |  |
| 12(c) | $20 \div$ their $2.5, \frac{6 \times 20}{15}$ | M1 | oe eg AB $\times$ their $2.5=20$ <br> ft from their (a) |
|  | 8 | A1ft | Accuracy to 1 dp or better |


| 13(a) | 27 | B1 |  |
| :--- | :--- | :--- | :--- |


| 13(b) | Comparison 1 on median | B1 | eg length are about same as medians are <br> similar. <br> Greenhouse cucumbers are longer on <br> average/as they have a higher median. |
| :---: | :--- | :---: | :--- |
|  | Comparison 2 on interquartile range <br> or range | B1 | Greenhouse cucumbers are more <br> consistent as range (or IQR) smaller. <br> Garden cucumbers are more varied as <br> range (or IQR) larger. |
|  | Use of relevant values from both box <br> plots for at least one comment. <br> Medians 28 and their 27 <br> IQR 11 and 15 <br> Range 26 and 33 | B1dep | eg medians are 1cm different <br> Greenhouse cucumbers are more <br> consistent with an IQR of 11 compared to <br> 15 |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 14(a) | $(x-3)(x+3)$ | B1 |  |
| :--- | :--- | :--- | :--- |


| 14(b) | $(a x \pm c)(b x \pm d)$ | M 1 | $a b=2, c d= \pm 3$ |
| :--- | :--- | :---: | :--- |
|  | $(2 x+1)(x-3)$ | A 1 |  |
|  | $\frac{x+3}{2 x+1}$ | A 1 ft | ft their (a) and factorisation of the <br> denominator providing there is a <br> common factors that can be cancelled <br> Contradictory further work award A0. |


| 15(a) | 4.5 or 7.5 or 5.5 as lower limit | B1 |  |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \frac{1}{2} \times(\text { their } 4.5+\text { their } 7.5) \times \text { their } 5.5 \\ & \frac{1}{2} \times(4.5+7.5) \times 6 \end{aligned}$ | M1 | Only award if consistent use of an 'lower limit', eg $\frac{1}{2} \times(4.9+7.9) \times 5.9$ |
|  | 33 | A1ft | ft on a consistent use for all 3 values of a sensible lower limit > 5 and given to at least 3 sf . <br> [Unlikely as this is a non-calc paper] <br> For example $\begin{array}{ll} . . .6 & 34.16 \\ \text {.. } 9 & 37.76 \\ \text {.. } 95 & 38.3775 \end{array}$ <br> whole numbers $4,7,5$ lead to 27.5 |


| 15(b) | $2 A$ as numerator | B1 |  |
| :--- | :--- | :---: | :--- |
|  | $a+b$ as part of denominator | B 1 | $h=$ is not essential |



| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| $\mathbf{1 7} \mathbf{1 7}$ | $2 \sqrt{ } 3$ or $5 \sqrt{ } 3$ seen | M1 |  |
|  | $7 \sqrt{ } 3$ | A1 |  |


| 18 | B1 fFor $64^{\frac{1}{3}}=4$ | B3 |  |
| :---: | :--- | :--- | :--- |
|  | B1 for $4^{\frac{3}{2}}=8$ |  |  |
|  | B1 for $27^{\frac{2}{3}}=9$ |  |  |


| 19 | $\frac{1}{3} \times \frac{1}{2} \times x \times x \times 2 x$ <br> or $\frac{1}{3} \times \frac{1}{2} \times C B \times D B \times A B(2 B C)$ | M1 | $\frac{1}{2} \times x \times x \times 2 x=24$ is M1 by implication. |
| :--- | :--- | :--- | :--- |
|  | $x^{3}=216$ | M1 |  |
| 6 | A1 | 6 from T\&I is 3 marks <br> 6 without verification or working is 1 mark. |  |


| 20 | $(x-2)$ or ( $x-4$ ) | M1 | $(x+2)$ and $(x+4)$ |
| :---: | :---: | :---: | :---: |
|  | $(x-2)(x-4)$ | M1dep | $(x+2)(x+4)$ |
|  | Evidence that brackets are expanded, ie $\left(x^{2}-2 x-4 x+\right) 8$ <br> or that the product of contant terms is taken. | M1dep | Dependent on $(x-2)(x-4)$ |
|  | 8 | A1 | But not from $(x+2)(x+4)$ <br> SC2 Answer only of 8 . <br> Minimum working for full marks is $-2 \times-4=8$ |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| Alt 1 <br> 20 | $0=2^{2}+2 a+b$ or $0=4^{2}+4 a+b$ | M1 | oe eg $-4=2 a+b$ |
| :---: | :---: | :---: | :---: |
|  | Evidence that variable is eliminated eg $2 a+12=0$ | M1dep | Evidence of balancing $a$ eg $0=8+4 a+2 b$ |
|  | Evidence of substituting back into an equation $\text { eg } 0=4+-12+b$ | M1dep | Dependent on second M1 only. Subtracting equations to eliminate $a$ |
|  | 8 | A1 |  |

